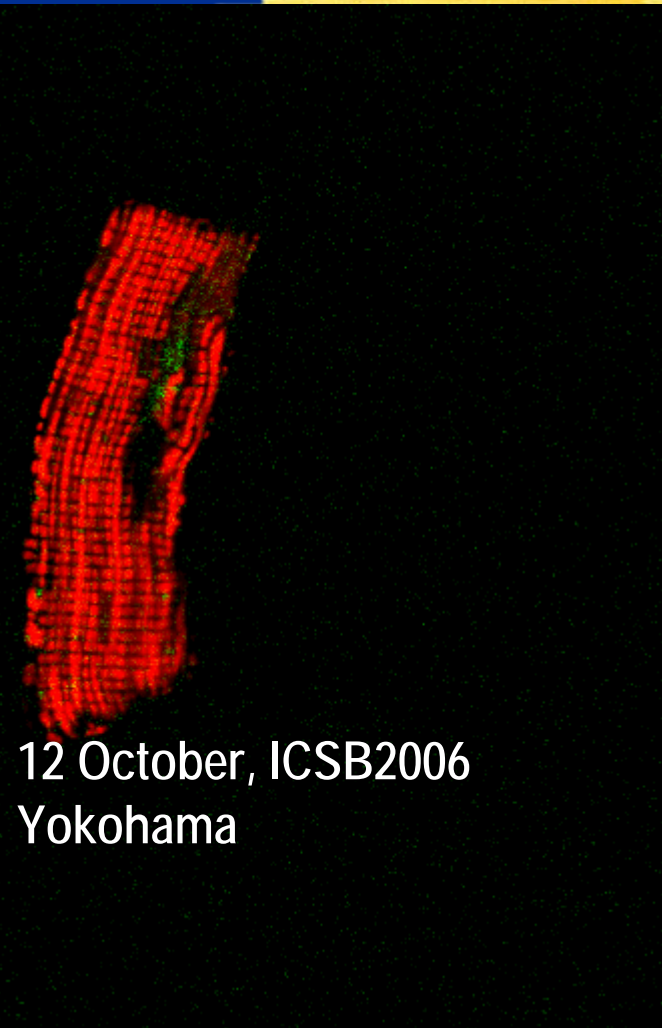
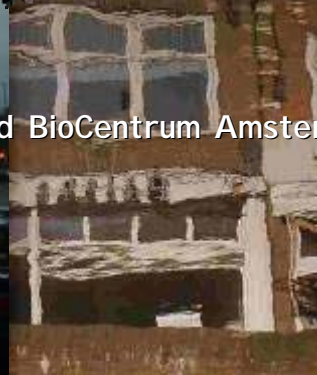
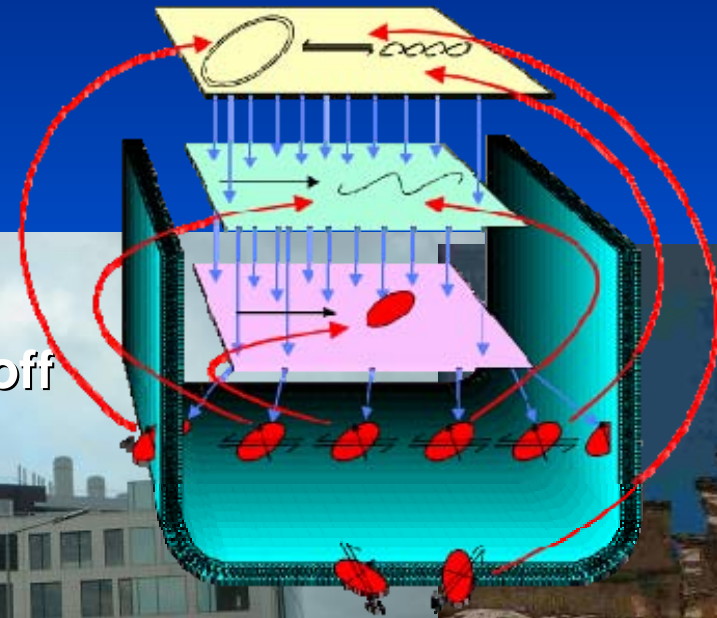


# Emerging Principles : a theory for robustness



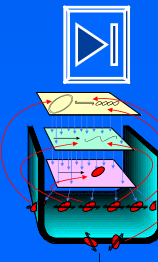
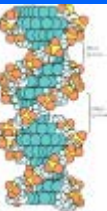
Hans V. Westerhoff  
and  
friends

Manchester Centre for Integrative Systems Biology and BioCentrum Amsterdam



# Opening lecture Hiroaki Kitano

- ⌘ We need a theory for systems biology, notably for robustness
- ⌘ Robustness is a system property
- ⌘ Is robustness conserved?
- ⌘ Trade-off between robustness and fragility (exact?)

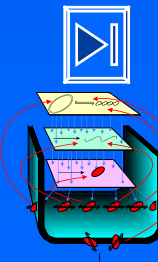
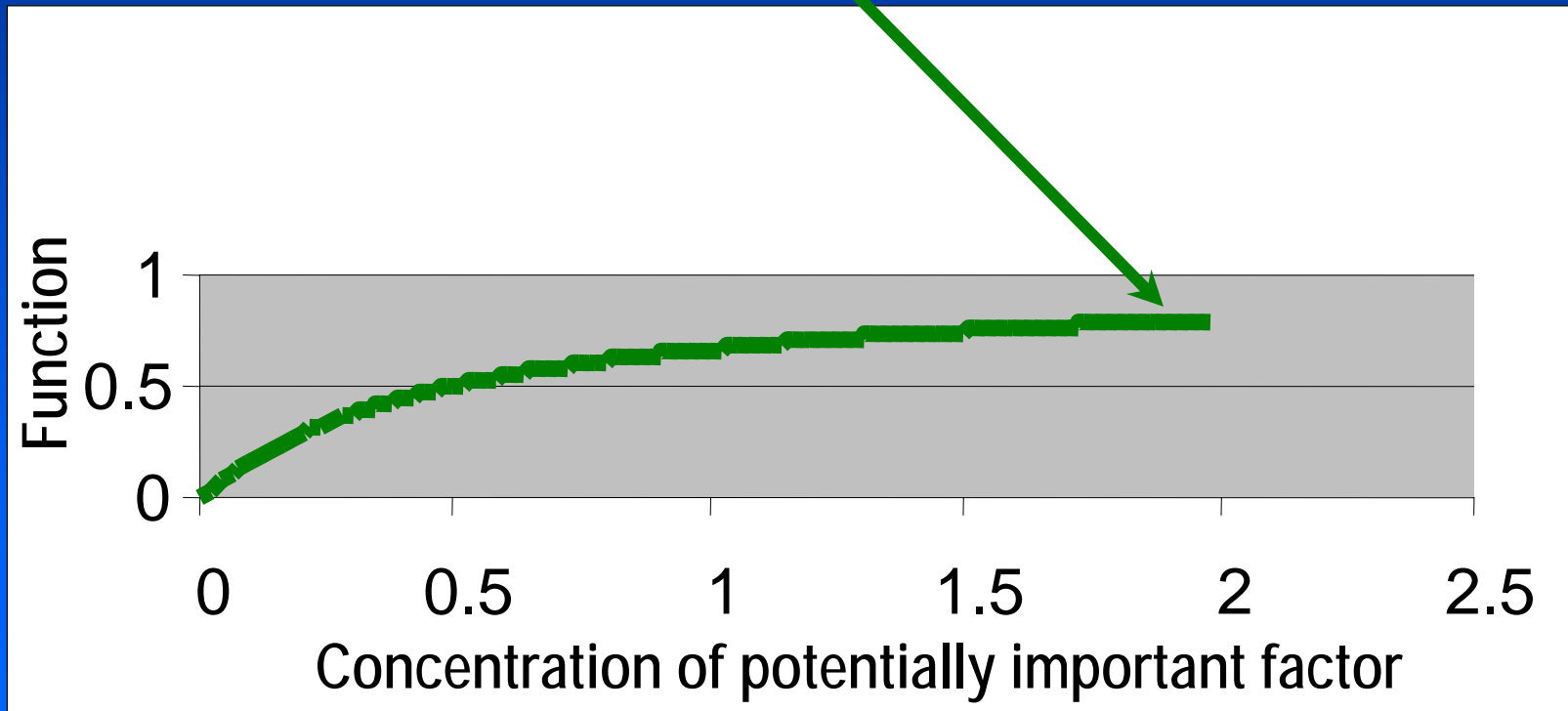


# For a theory of robustness



We need a definition of  
robustness

# An example of robustness



# Definition of robustness *vis-à-vis* a perturbation

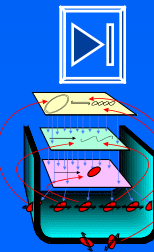
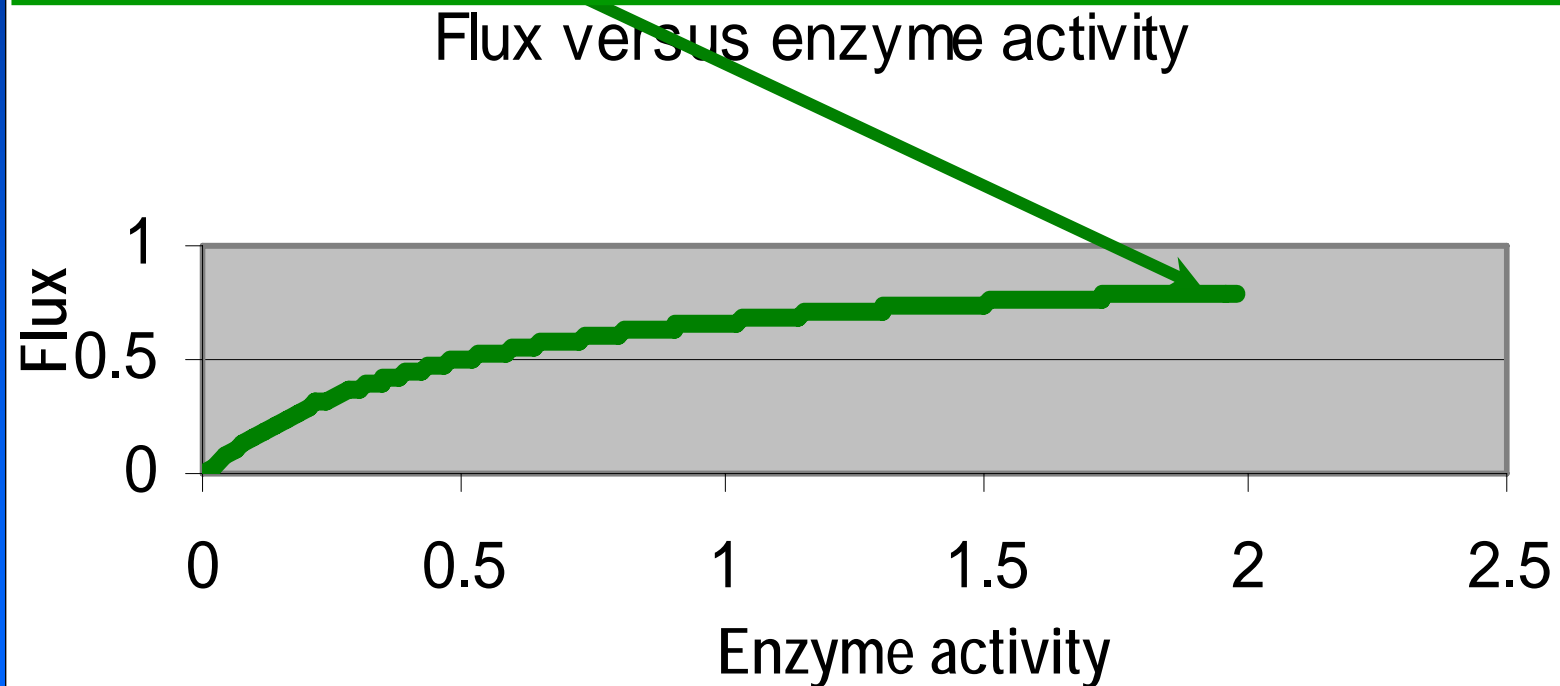
---

How robust is a function with respect to a perturbation in a property?

**By what percentage can I perturb that property and still affect system function by only 1 %?**

# An example of robustness

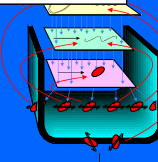
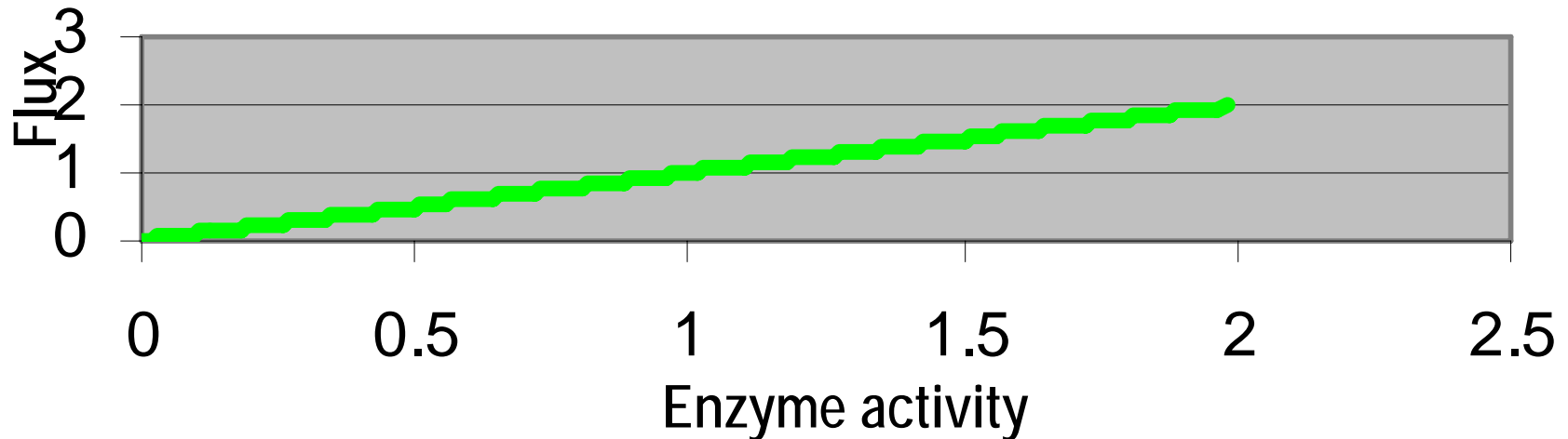
$$\mathcal{R}_{e_i}^J \equiv \frac{5\% \text{ decrease in enzyme activity}}{1\% \text{ decrease in function (flux) } J} = 5$$



Robustness is a system property:  
Low robustness of processes in isolation

$$\mathcal{R}_{e_i}^J \equiv \frac{1\% \text{ decrease in enzyme activity}}{1\% \text{ decrease in function (flux) } J} = 1$$

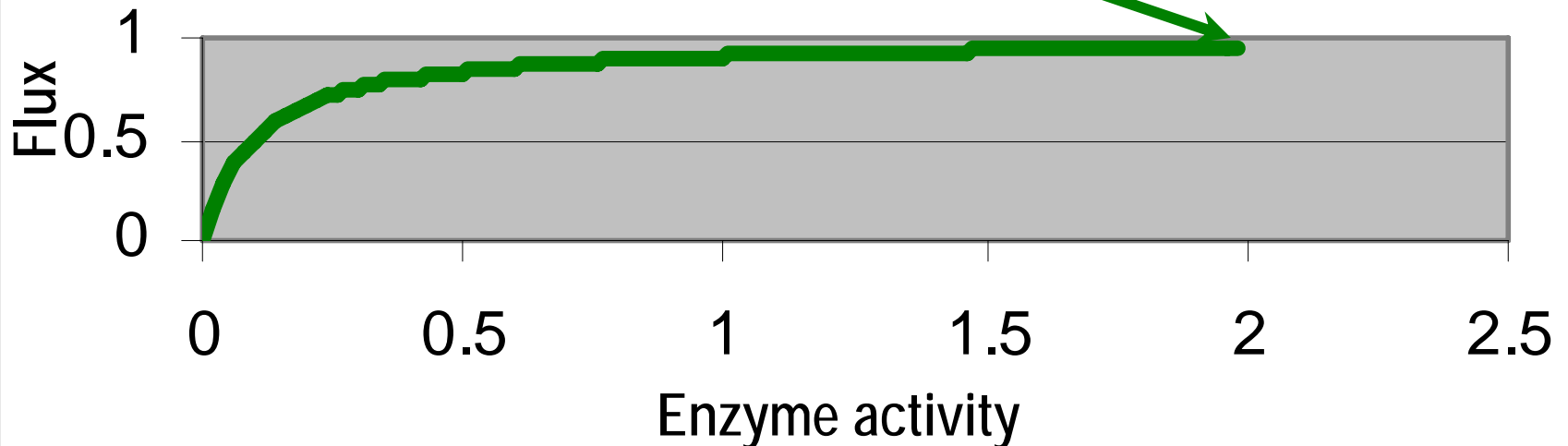
Flux versus enzyme activity



# An example of high robustness

$$\mathcal{R}_{e_i}^J \equiv \frac{23\% \text{ decrease in enzyme activity}}{1\% \text{ decrease in function (flux) } J} = 23$$

Flux versus enzyme activity

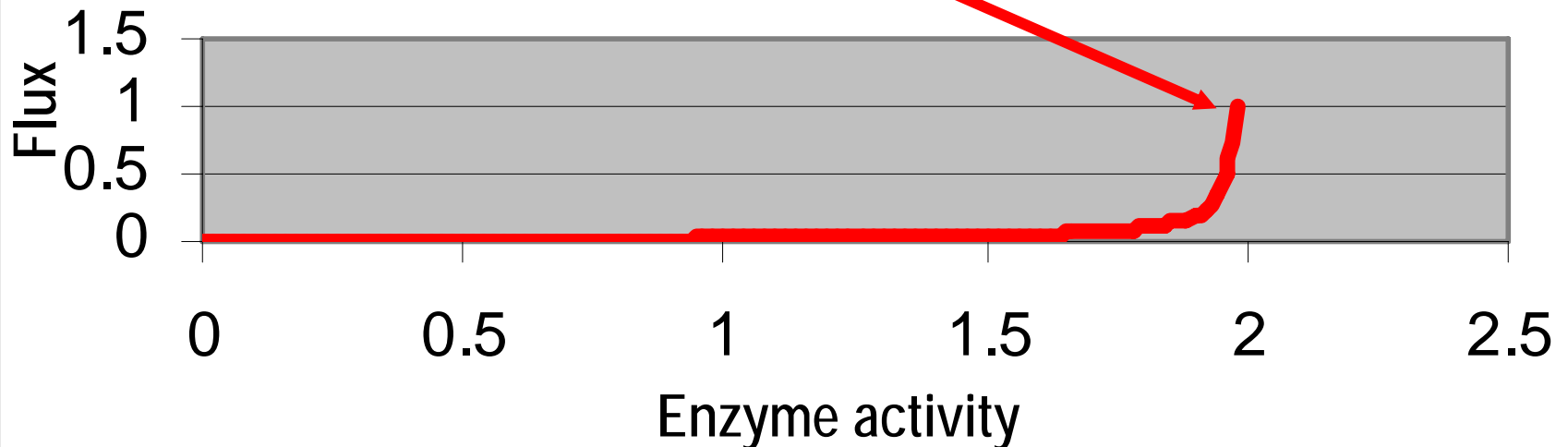




# An example of lack of robustness (fragility)

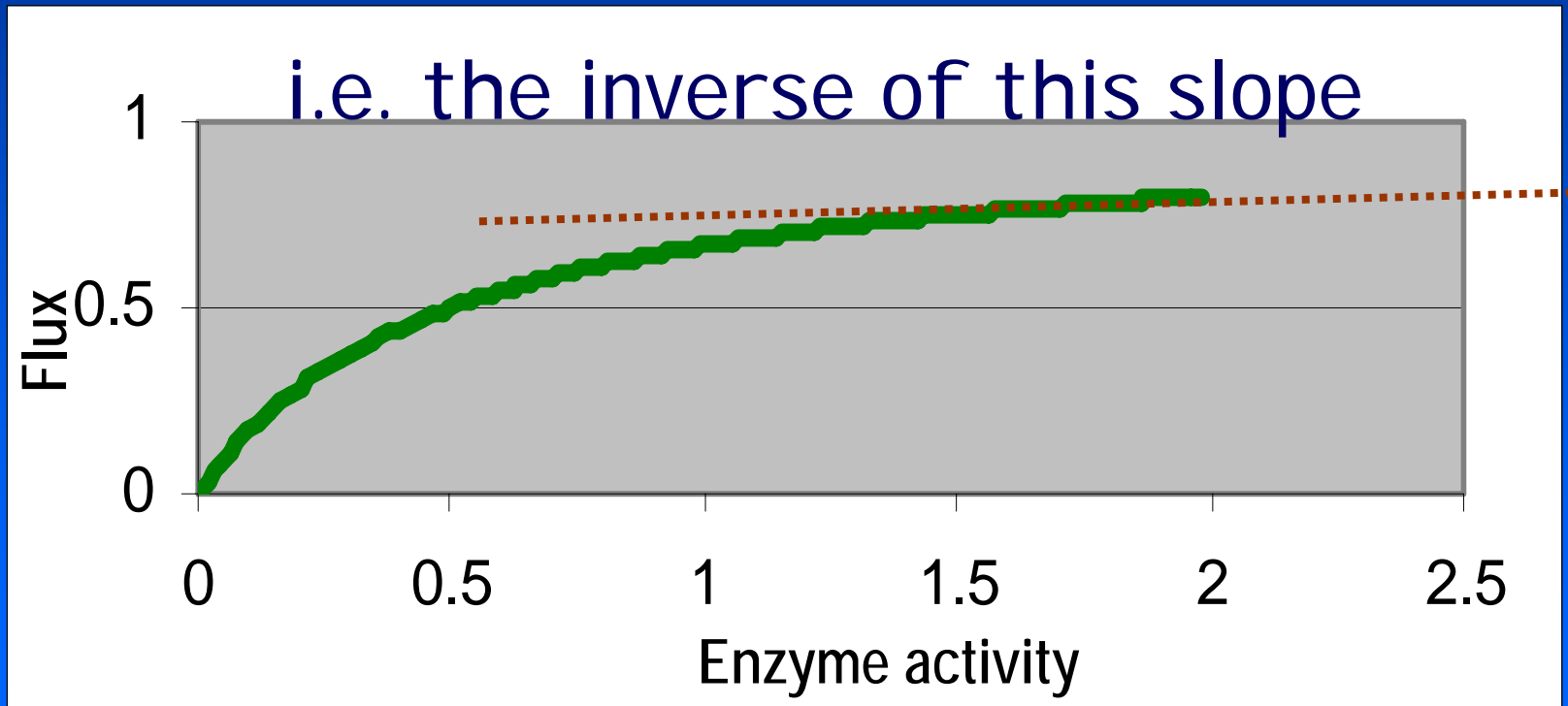
$$\mathcal{R}_{e_i}^J \equiv \frac{0.1\% \text{ decrease in enzyme activity}}{1\% \text{ decrease in function (flux) } J} = 0.1$$

Flux versus enzyme activity



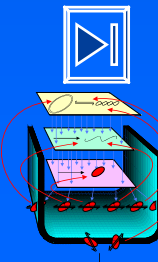
# More precise definition of robustness

$$\mathfrak{R}_{e_i}^{function_j} \equiv \left( \frac{\partial enzyme_i / enzyme_i}{\partial function_j / function_j} \right)_{\text{all other parameters}} = \left( \frac{\partial \ln enzyme_i}{\partial \ln function_j} \right)_{\text{all other parameters}} = 1 / \left( \frac{\partial \ln function_j}{\partial \ln enzyme_i} \right)_{\text{all other parameters}}$$



# Robustness

- ⌘ There is more than one definition
- ⌘ E.g. John Doyle's definition: frequency domain
- ⌘ This one: steady state function with respect to parameters, such as catalytic activities



# Are robustnesses large?

## Silicon cell live models: [jij.bio.vu.nl](http://jij.bio.vu.nl)

JWSapplet: Glycolysis in *Trypanosoma brucei* - Bakker et al.

[Home](#)

[Model Database](#)

[Site information](#)

[Contact info](#)

[sbml](#)

JWSapplet - ver 4.1.1 Bakker

	Parameter	Value
P28_v1	Vm7	1.
P29_v1	K7GAP	0.15
P30_v1	K7NAD	0.45
P31_v1	K7NADH	0.02
P32_v1	K7BPGA13	0.1
P33_v1	Vm8f	533
P34_v1	Vm8r	149.24
P35_v1	Vm8	1.
P36_v1	K8DHAPg	0.1
P37_v1	K8NADH	0.01
P38_v1	K8NAD	0.4
P39_v1	K8Gly3Pg	2
P40_v1	Vm9	18
P41_v1	K9Gly3Pc	1.7
P42_v1	Vm10	200
P43_v1	K10Pyr	1.96
P44_v1	Vm11f	640
P45_v1	Vm11r	18.56
P46_v1	Vm11	1.
P47_v1	K11BPGA13	0.05

Evaluate Model

Sim State MCA

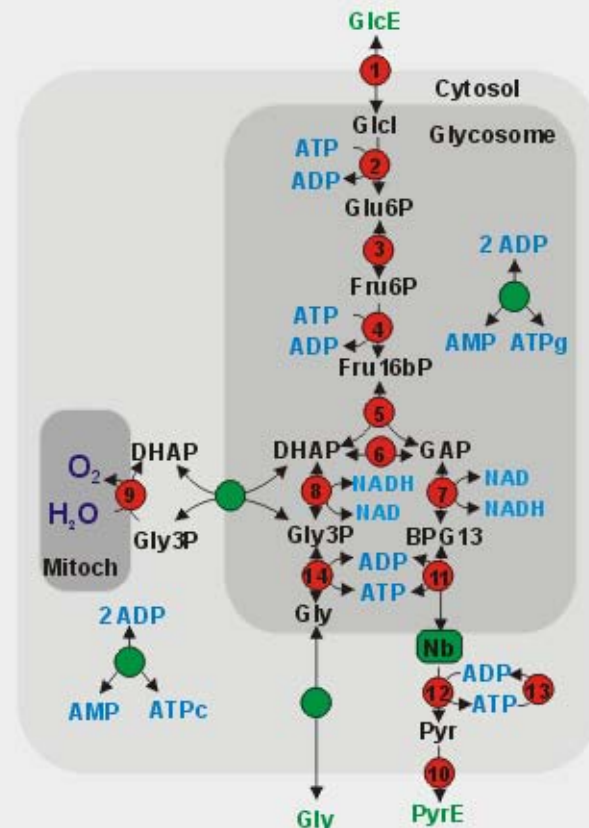
Steady-State Analyse

- Steady State
- N matrix:  $ds/dt=N*v$
- K matrix:  $J=K*Ji$
- L matrix:  $s=L*si+T$
- Jacobian:  $d(ds/dt)/ds$
- Eigenvalues

POWERED BY webMATHEMATICA2

Moi

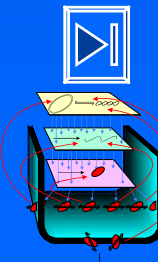
Reset



# Robustness of vital flux of Trypanosomes *vis-à-vis* perturbation of various glycolytic steps

step	Robustness
Glctr	1.1
GAPdh	42
HK	42
PGI	1546
PFK	234
ALD	38
TPI	482
GDH	66
GPO	-251
PGK	61
PK	691
ATPase	2744
GlyK	389

Yes, most  
robustnesses are  
large; average is 468  
here



# Systems Biology: principles



Are there any principles vis-à-vis  
this robustness?

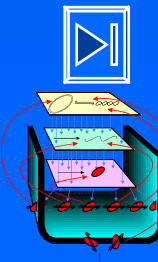
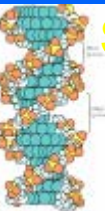
Is robustness conserved?

# Is robustness conserved?

(e.g. when making the most fragile step robust)

step	Robustness	Robustness double glc transporter
Glctr	1.1	88
GAPdh	42	4
HK	42	20
PGI	1546	412
PFK	234	56.
ALD	38	3
TPI	482	64
GDH	66	6
GPO	-251	-15
PGK	61	7
PK	691	73
ATPase	2744	313
GlyK	389	26
<b>Sum (average)</b>	<b>6085 (468)</b>	<b>1055(81)</b>

No, robustness is not conserved



No principles then?

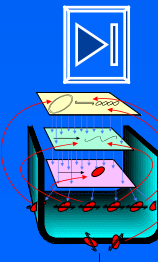


Yes, there is one!



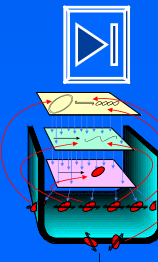
# Sum over all inverse robustnesses = 1

step	1/robustness	1/robustness (doubled glc transporter)
GlcTr	0.887	0.011
GAPdh	0.024	0.249
HK	0.024	0.051
PGI	0.001	0.002
PFK	0.004	0.018
ALD	0.026	0.354
TPI	0.002	0.016
GDH	0.015	0.166
GPO	-0.004	-0.068
PGK	0.016	0.144
PK	0.001	0.014
ATPase	0	0.003
GlyK	0.003	0.039
<b>Sum</b>	<b>0.999</b>	<b>0.999</b>



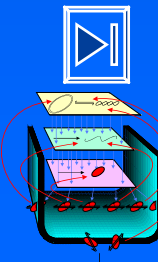
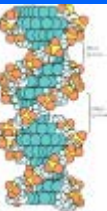
# Systems Biology principle concerning robustness

$$\sum_{i=1}^n \frac{1}{\mathcal{R}_{e_i}^J} \equiv 1$$



# Implications

- ⌘ Flux robustnesses can be homogeneous (robustness the same *vis-à-vis* all enzyme perturbations) or heterogeneous
- ⌘ Average robustness is higher when robustness is heterogeneous
- ⌘ By increasing fragility *vis-à-vis* one step one can increase the average robustness
- ⌘ Lowest robustness is best drug target



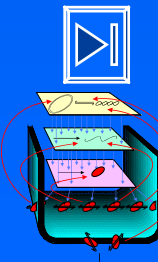
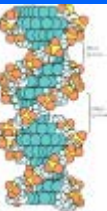
# Opening lecture Hiroaki Kitano

⌘ We need a theory for systems biology, notably for robustness 

⌘ Robustness is a system property 

⌘ Is robustness conserved? 

⌘ Trade-off between robustness and fragility  (exact?) 

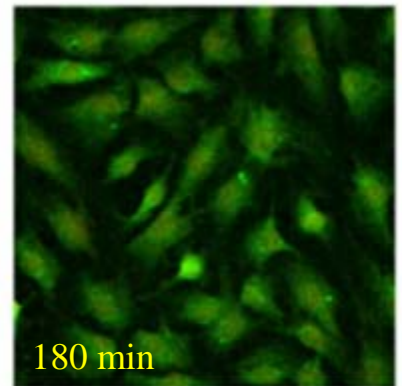
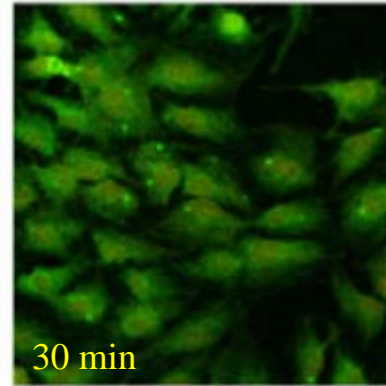
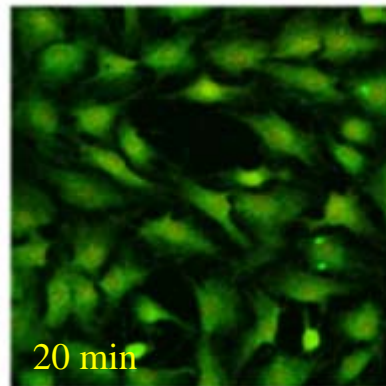
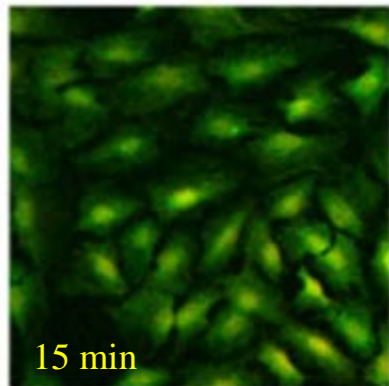
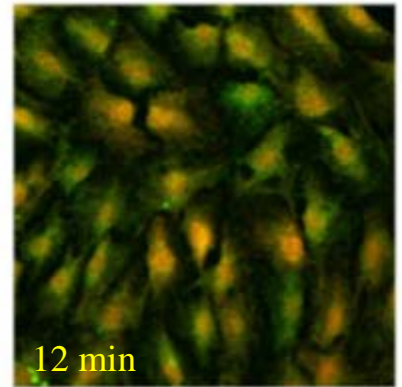
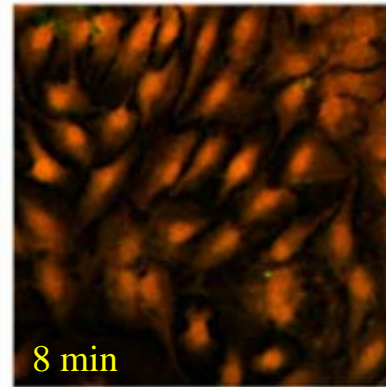
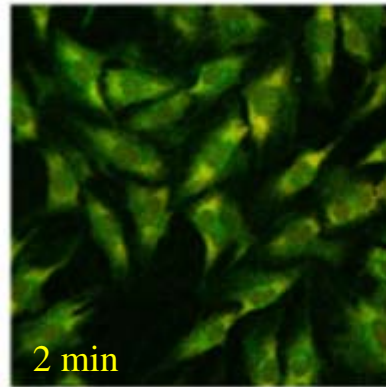
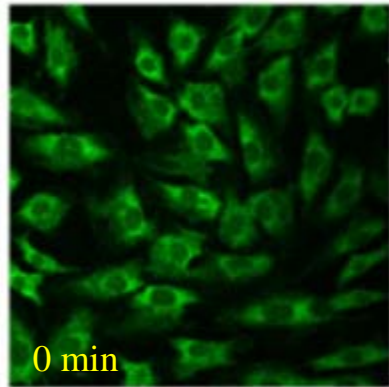


# Robustness of ERK phosphorylation



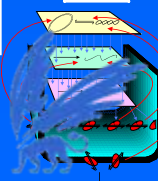
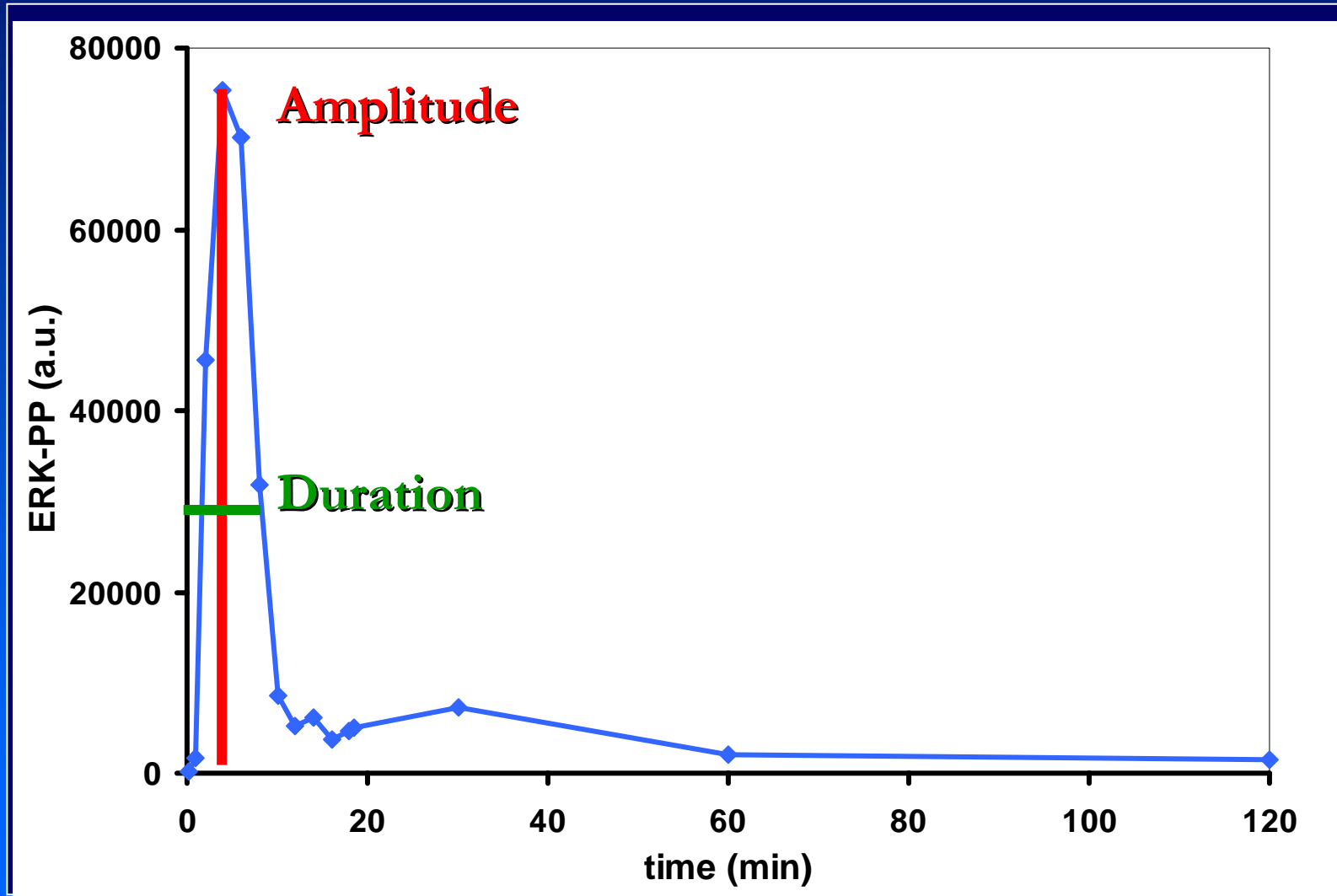
EGF initiated signal  
transduction

# ERK-PP in single cells upon EGF stimulation



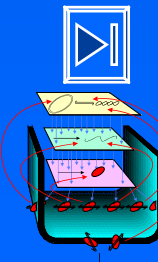
Green: total ERK  
Red: ERK-PP

# ERK-PP profile upon EGF stimulation



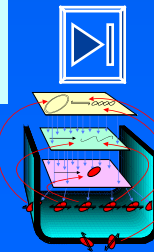
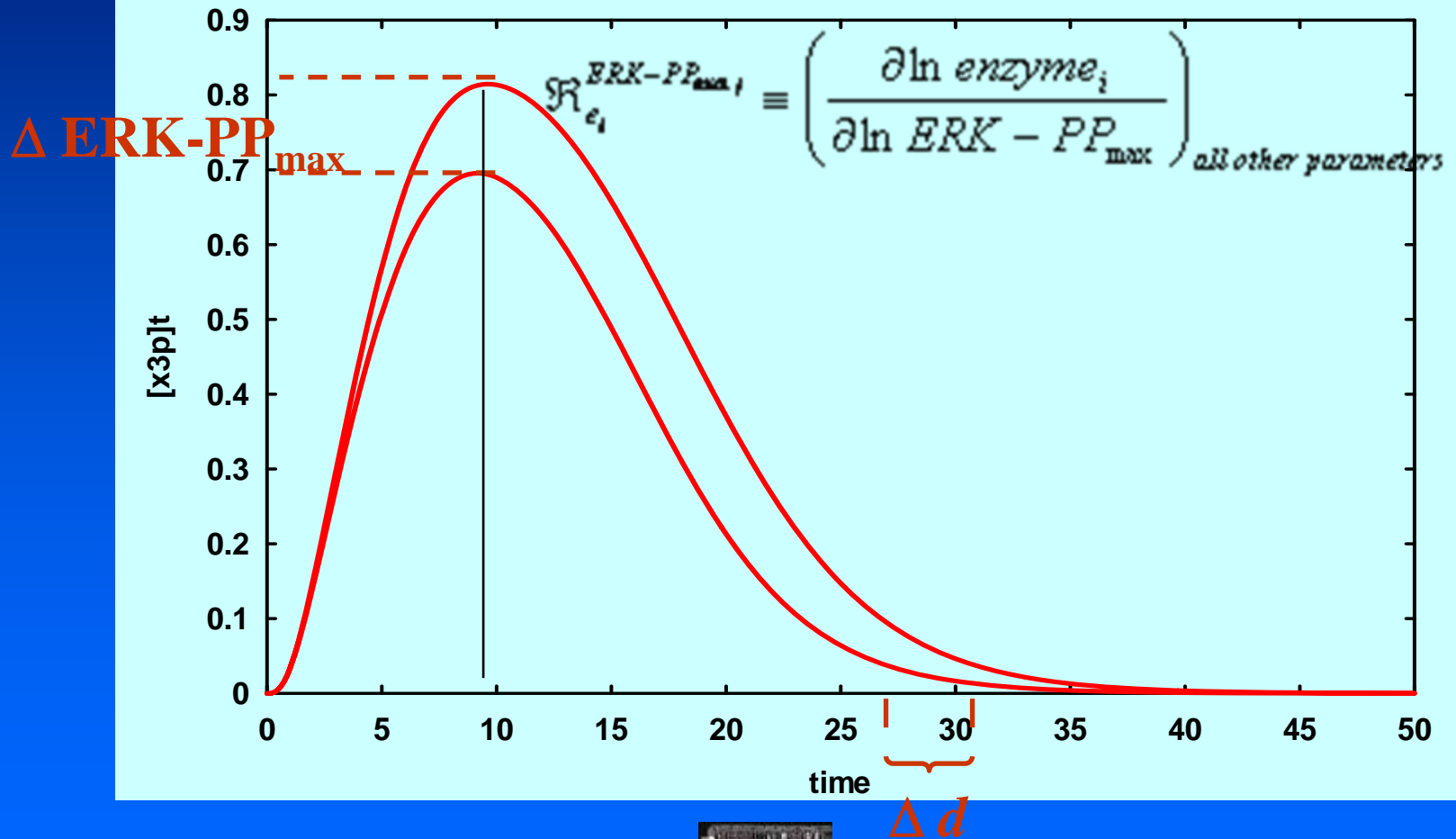
# Research questions

- ⌘ To which perturbations is this signal transduction robust (fragile)?
- ⌘ Does this differ for the various aspects of the signal?
- ⌘ Are there generic principles here?





# Robustness of ERK-PP *vis-à-vis* perturbation

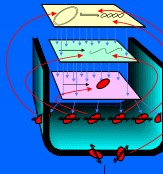
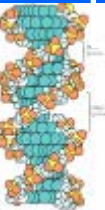


# Robustness of ERK-PP amplitude in model MAP kinase pathway: mostly robust

	kinases			phosphatases				Sum
	1	2	3	1	2	3	R	
Amplitude	6	4	2	-7	-5	-3	-6	-9

33

52

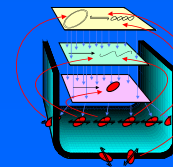


# Duration robustness in model MAP kinase pathway

	kinases			phosphatases				Sum
	1	2	3	1	2	3	R	
Amplitude	6	4	2	-7	-5	-3	-6	-9
Duration	<b>17</b>	<b>11</b>	<b>8</b>	<b>-2</b>	<b>-3</b>	<b>-3</b>	<b>-8</b>	<b>20</b>

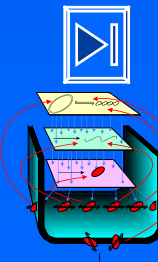
33

52



# Research questions

- ⌘ To which perturbations is this signal transduction robust (fragile)? **Most**
- ⌘ Does robustness differ for the various aspects of the signal?
- ⌘ Are there generic principles here?

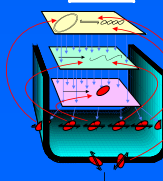
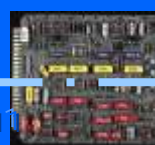
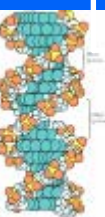


# Robustness depends on function considered and is not conserved

	kinases			phosphatases				Sum
	1	2	3	1	2	3	R	
Amplitude	6	4	2	-7	-5	-3	-6	-9
Duration	17	11	8	-2	-3	-3	-8	20

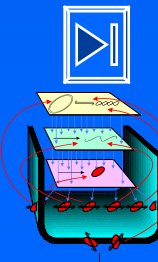
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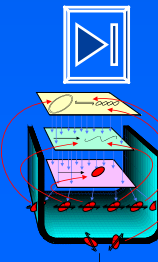
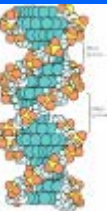
# Systems Biology principle concerning robustness

$$\sum_{i=1}^n \frac{1}{\mathcal{R}_{e_i}^{amplitude}} \equiv 0$$



# Research questions

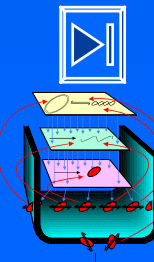
- ⌘ To which perturbations is this signal transduction robust (fragile)? **Most**
- ⌘ Does robustness differ for the various aspects of the signal? **Yes**
- ⌘ Are there generic principles here? **Yes**



# Systems Biology principles concerning robustness differ

$$\sum_{i=1}^n \frac{1}{\mathcal{R}_{e_i}^{amplitude}} \equiv 0$$

$$\sum_{i=1}^n \frac{1}{\mathcal{R}_{e_i}^{duration}} \equiv -1$$





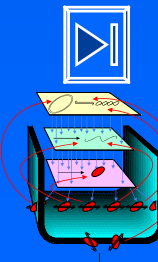
Incidentally, the math behind  
these theorems....



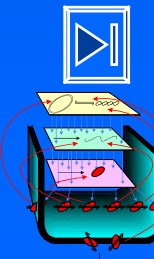
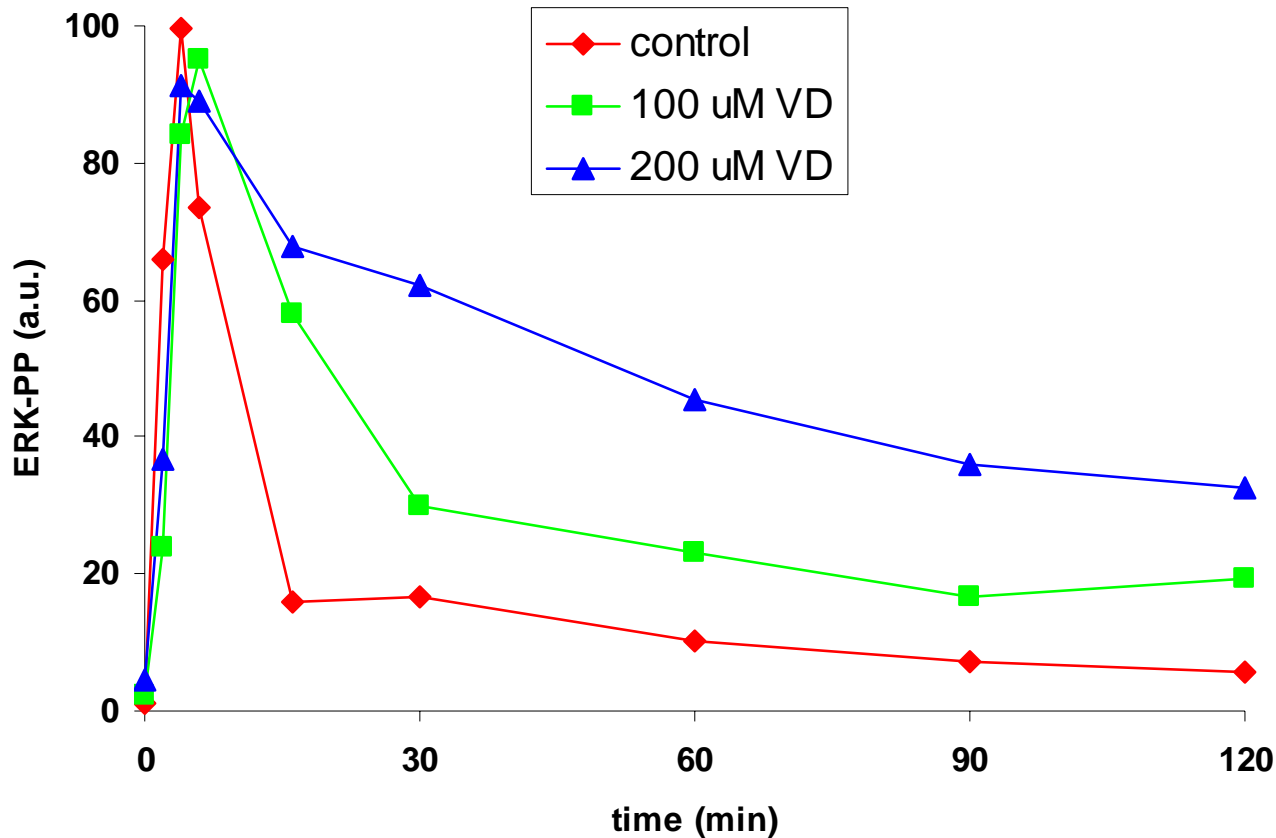
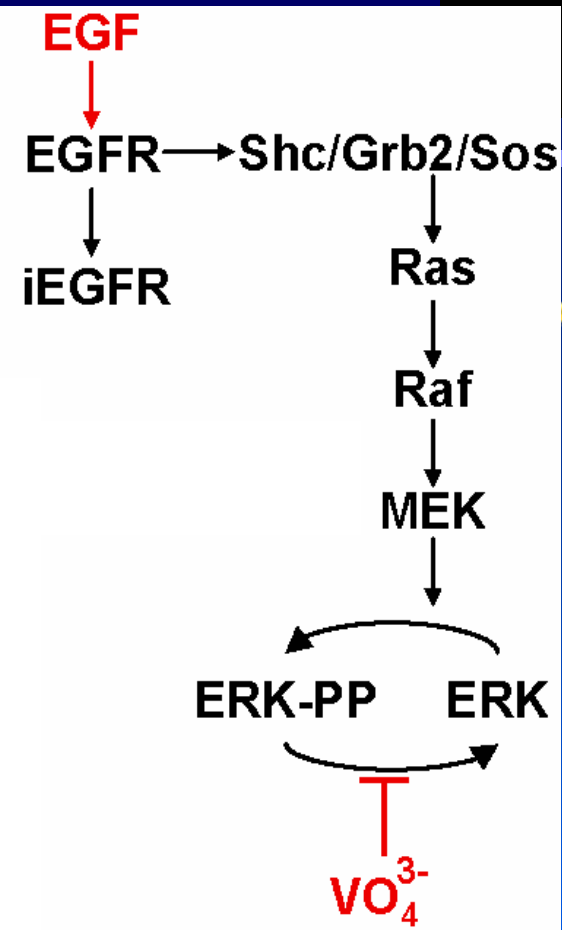
Metabolic Control Analysis

# Fragility *vis-à-vis* kinases and phosphatase perturbation?

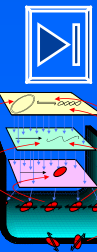
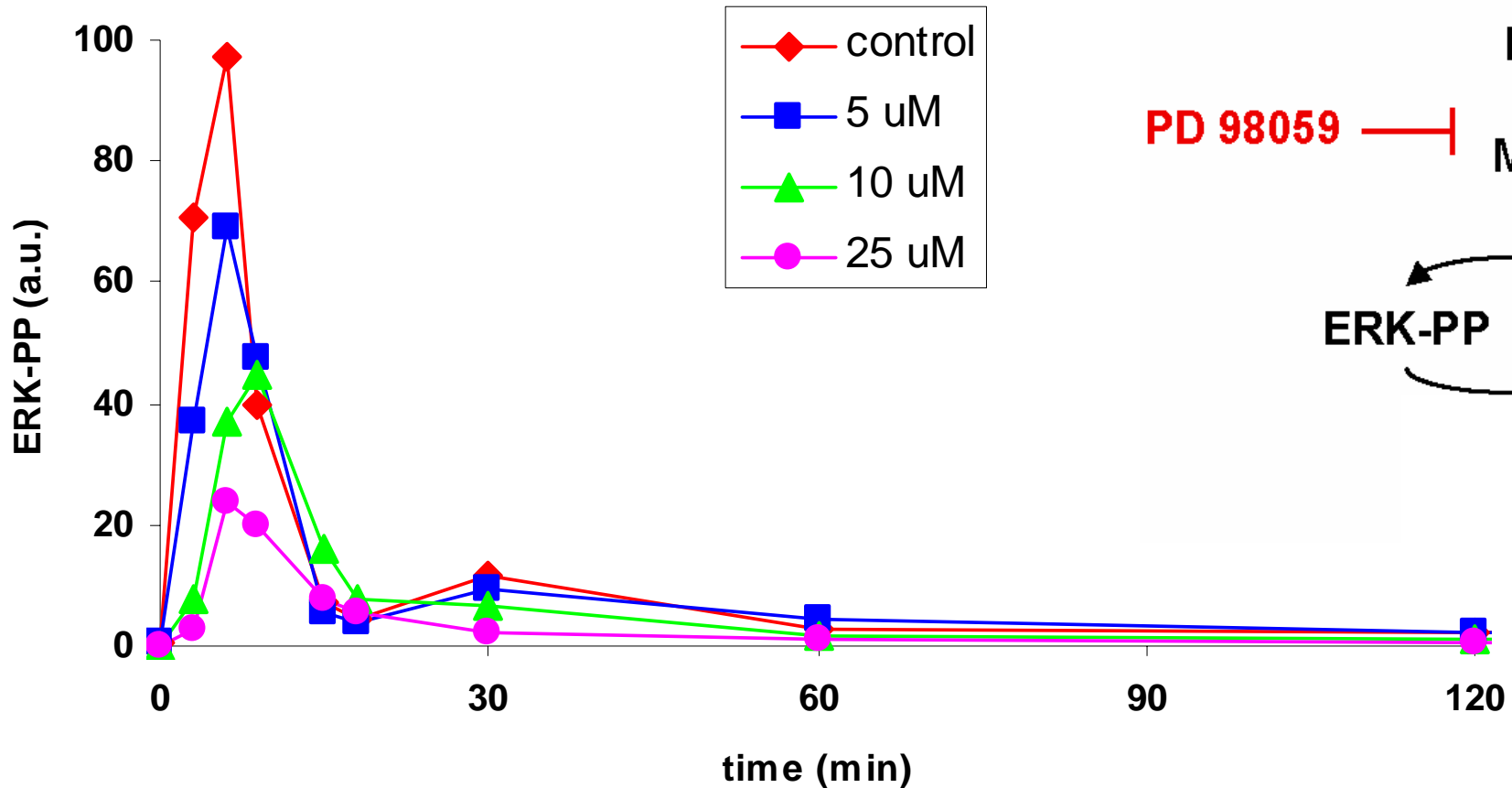
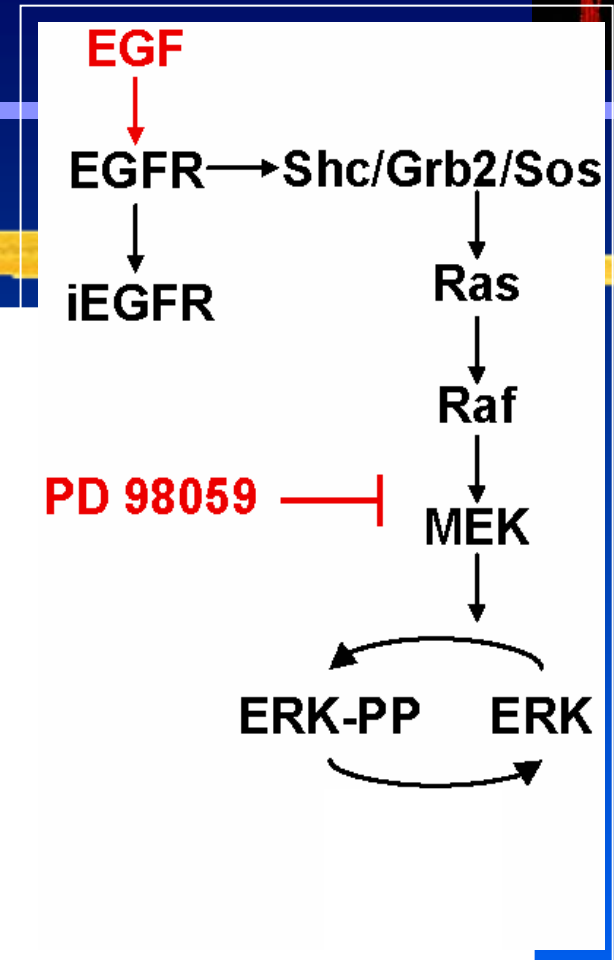
- ⌘ Duration more than amplitude is fragile *vis-à-vis* phosphatase perturbation
- ⌘ Amplitude more than duration is fragile *vis-à-vis* kinase perturbation



Duration more than amplitude is fragile *vis-à-vis* phosphatases



Amplitude more than duration is fragile *vis-à-vis* kinases



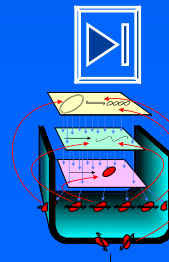
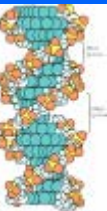
# Is it all true?

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⌘ Duration fragility resides more in phosphatases

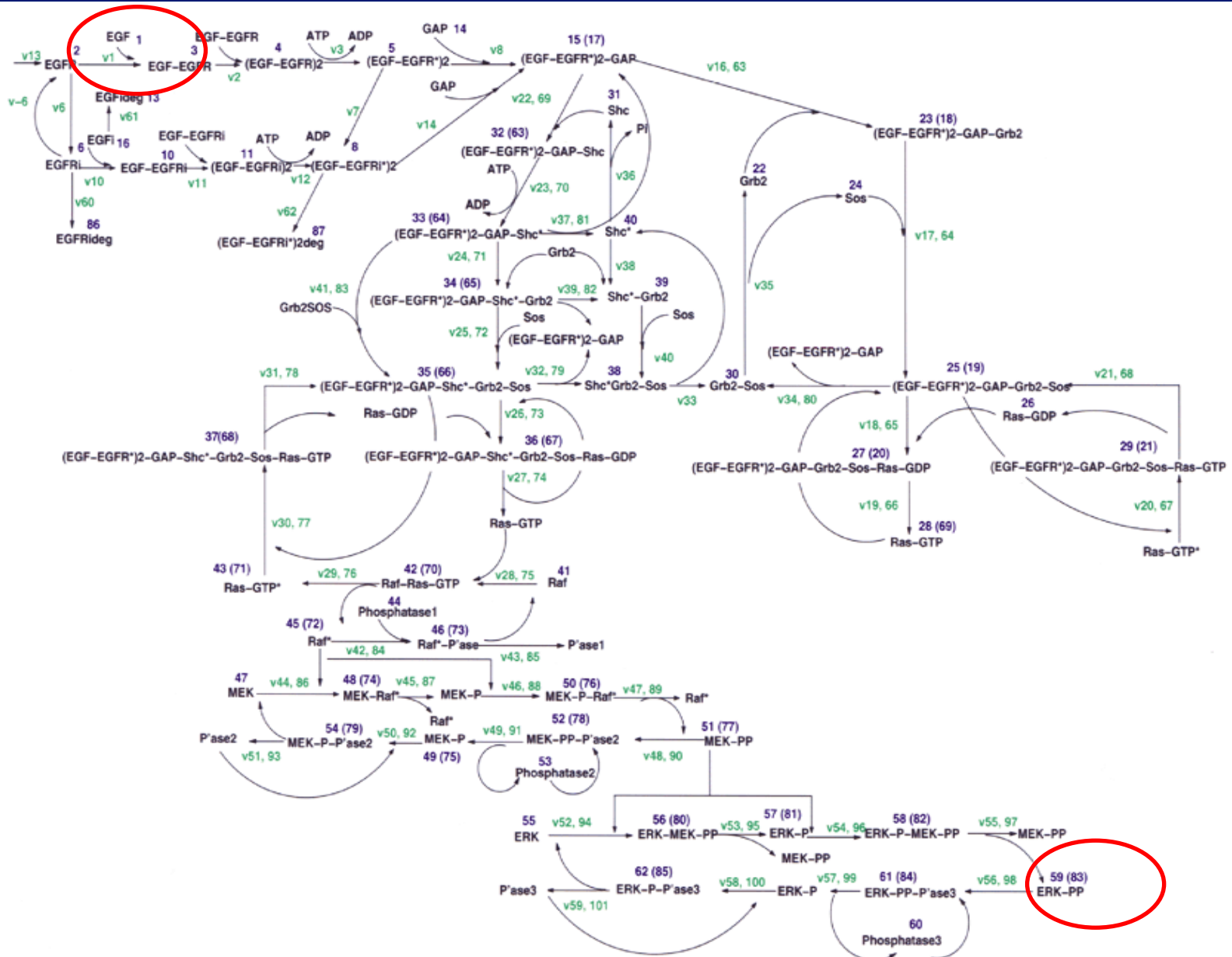


⌘ Amplitude more fragile vis-à-vis kinase activity

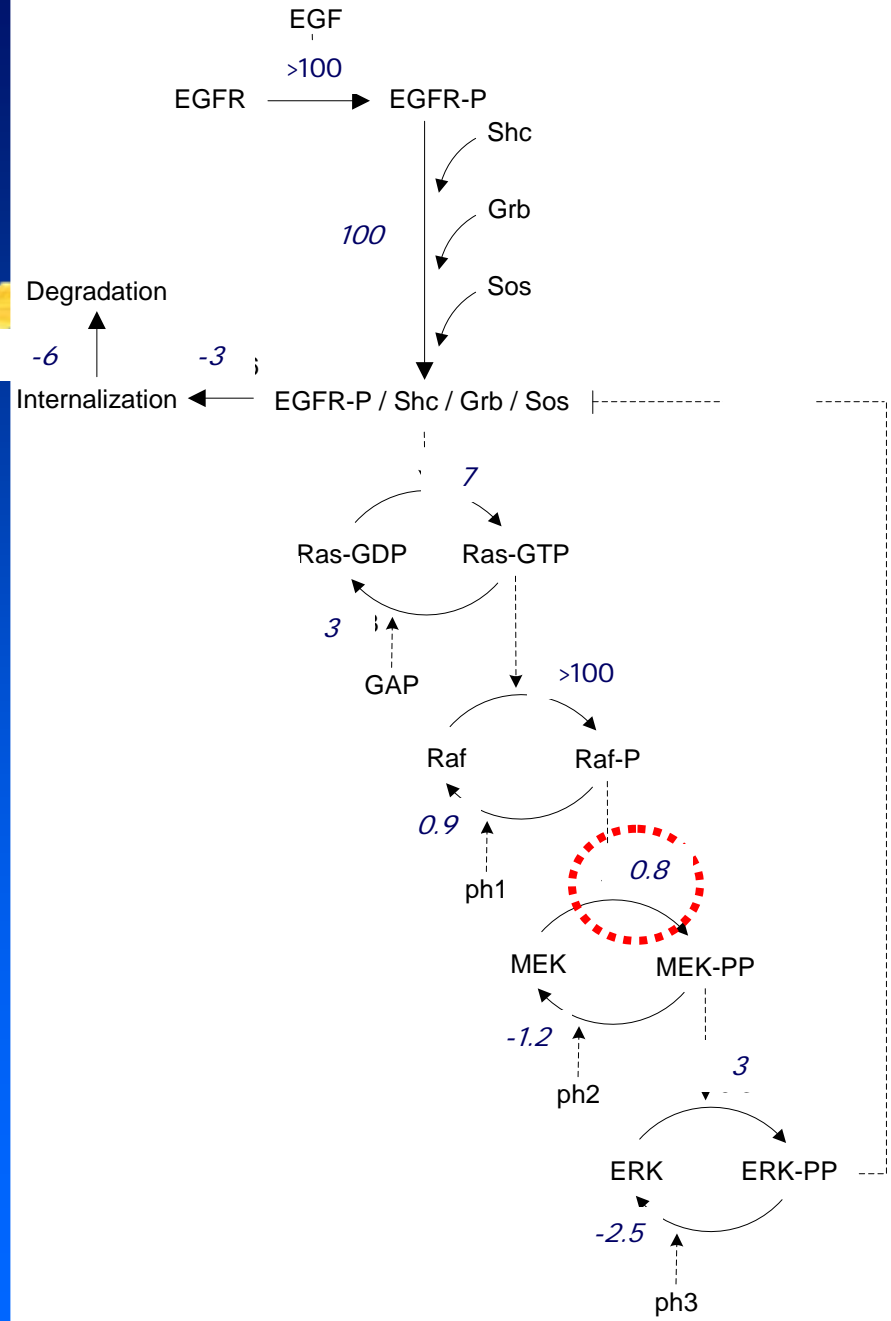


# Detailed kinetic model of signaling by EGF

Schoeberl *et al.* (2002)



# MAP kinase signaling: which steps are robust?



## Mutations of the *BRAF* gene in human cancer

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**Oncogenes affect steps for which the system is least robust**



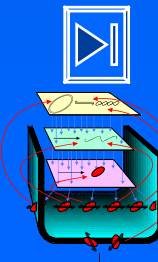
**And increase the robustness**

**Tumor cell is more robust**



# Emerging Principles of Living Systems: Robustness

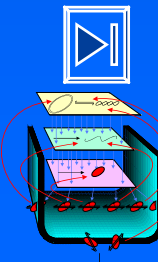
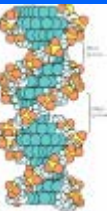
- ⌘ Robustness, a quantitative definition
- ⌘ Example: robustness of the vital flux of Trypanosomes
  - ⌘ Robustness is not conserved
  - ⌘ General principle 1: fluxes
- ⌘ Robustness in signal transduction 
  - ⌘ General principle 2: amplitude
  - ⌘ Duration fragile *vis-à-vis* phosphatases perturbation more than kinase perturbation
  - ⌘ Amplitude also fragile *vis-a-vis* kinase perturbation
- ⌘ Oncogenes: may act to enhance robustness



# Opening lecture Hiroaki Kitano

- ⌘ We need a theory for systems biology, notably for robustness
- ⌘ Robustness is a system property
- ⌘ Is robustness conserved?
- ⌘ Trade-off between robustness and fragility (exact?)

⌘ **Hiroaki was right!**

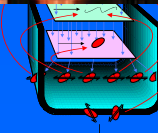
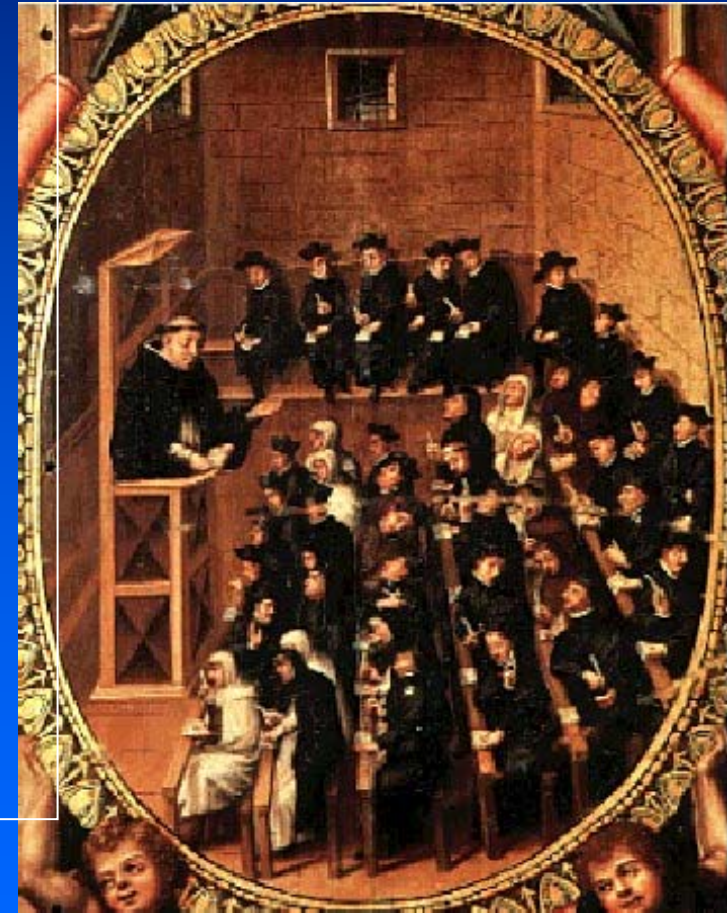


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**and many others**

Barbara Bakker  
Frank Bruggeman  
Reinhart Heinrich  
Jorrit Hornberg



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